

*AsCA meeting,  
6 December 2025*



# Molecular Replacement

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# Crystallography: Phase problem

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$$\rho(\mathbf{r}) = \frac{1}{V_{cell}} \sum_{hkl} |F(hkl)| e^{i\alpha} e^{-2\pi i \mathbf{h} \cdot \mathbf{r}}$$

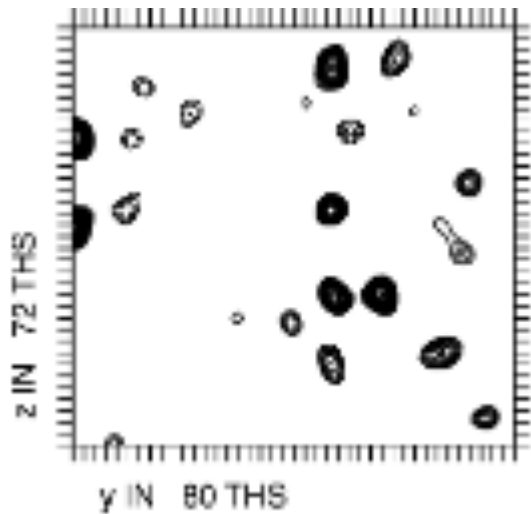
amplitude                      phase

Measured in diffraction  
experiment

Not measured

# How to recover phases in Crystallography

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## Experimentally

Exploit the properties of a few special atoms:

- Anomalous scattering
- A large number of electrons

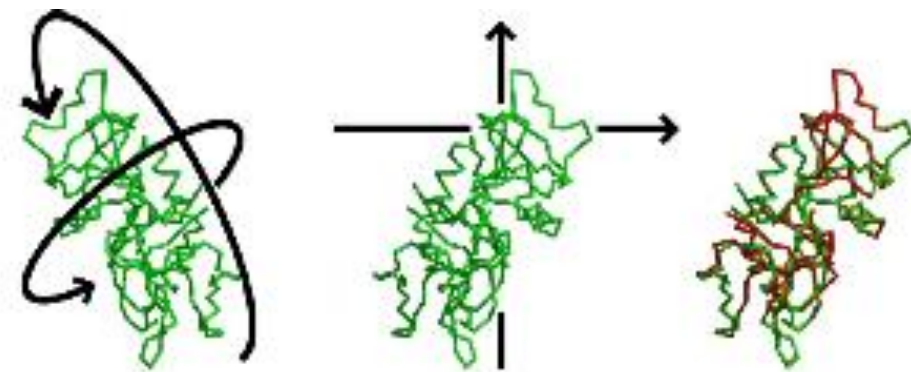
## Computationally

- *Molecular Replacement (MR)*

A previously known structure provides initial phase estimates for a new structure

- *Direct Methods*

Phase relationships can be formulated by assuming the positivity and atomicity of the electron density



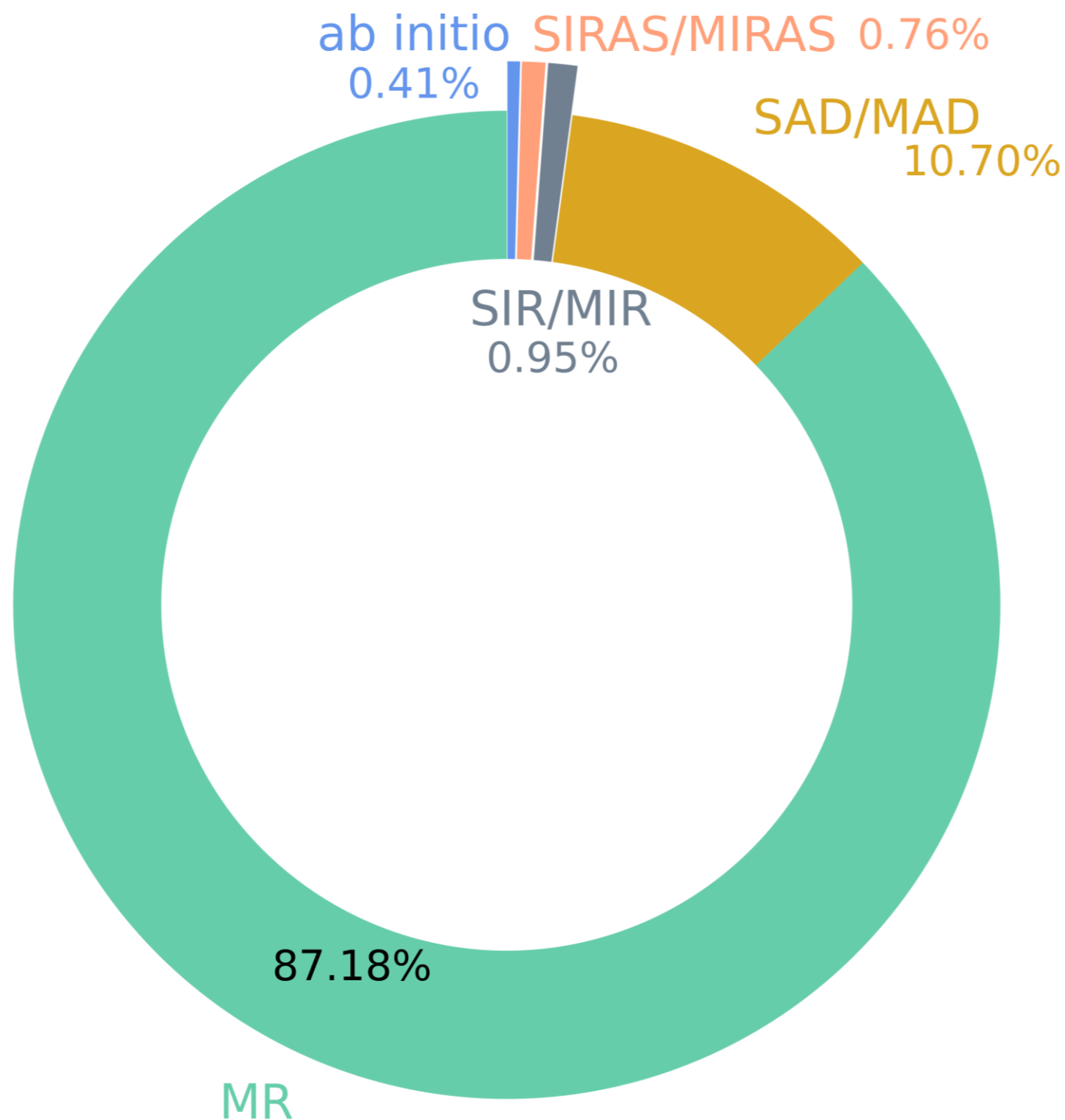
# How to recover phases in Crystallography

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Method	Source of phasing information
SIR – single isomorphous replacement	A few heavy atoms (e.g., Hg, Au) in “derivative” contribute to differences from “native”
SAD – single-wavelength anomalous diffraction	A few atoms (e.g., Se, I, Hg atoms) contribute to “anomalous” differences in diffraction between spot $h$ and spot $-h$
MAD – multiple-wavelength anomalous diffraction	A few atoms contribute to anomalous and wavelength-dependent “dispersive” differences
SIRAS, MIR	Combinations of SIR and SAD
Molecular replacement	Molecular location and phases are found using a related molecule as a template
Direct methods	Guess where atoms are, good guesses match the measured structure factors

# Phasing methods in the PDB

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## MR method:

- Fast
- Cheap
- Highly automated

## Known structure:

- Large number of deposited structures (PDB: 234k)
- Predicted models

Note: Not all models in the PDB have info, and even if present, it may not represent major phasing method.

# Molecular Replacement (MR)

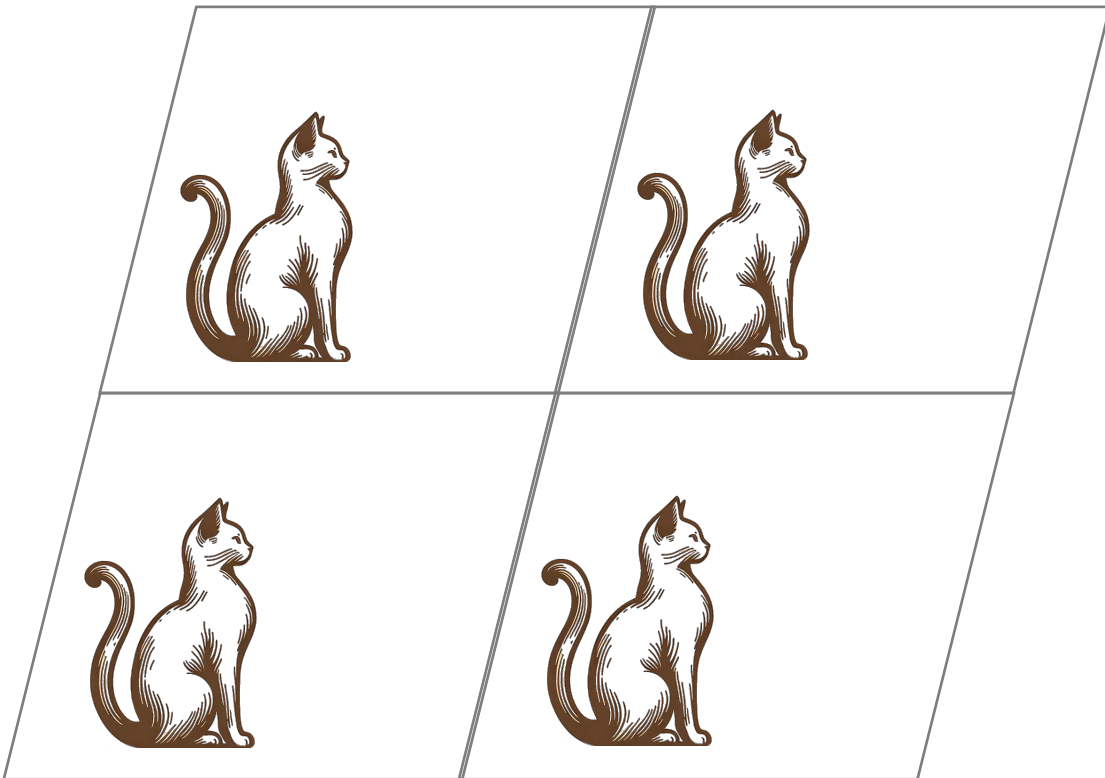
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MR = solve the **unknown** crystal structure of a molecule using a related **known molecular model**.

Known model



Crystal of unknown structure



# Molecular Replacement (MR)

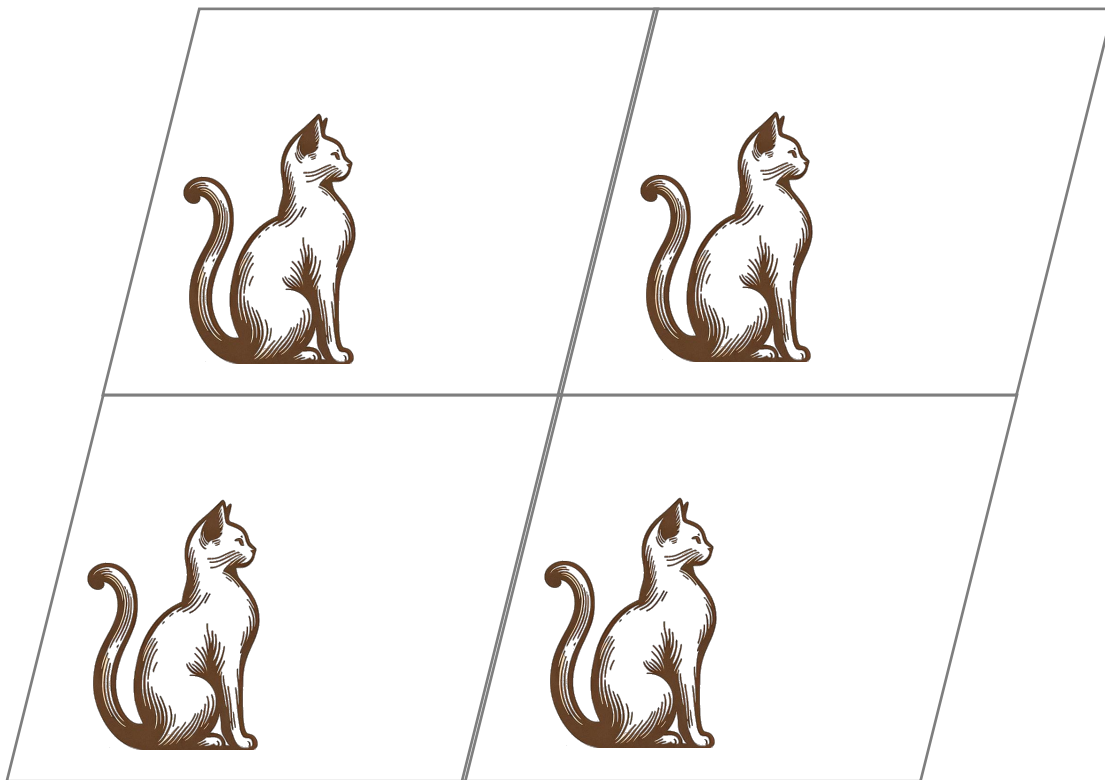
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MR = solve the **unknown** crystal structure of a molecule using a related **known molecular model**.

Known model



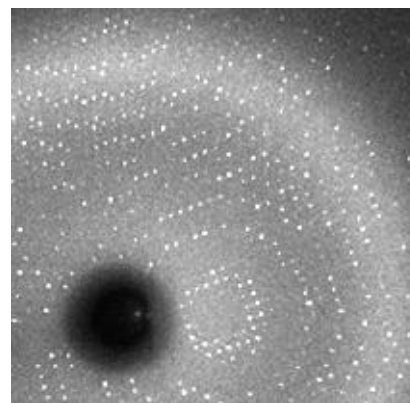
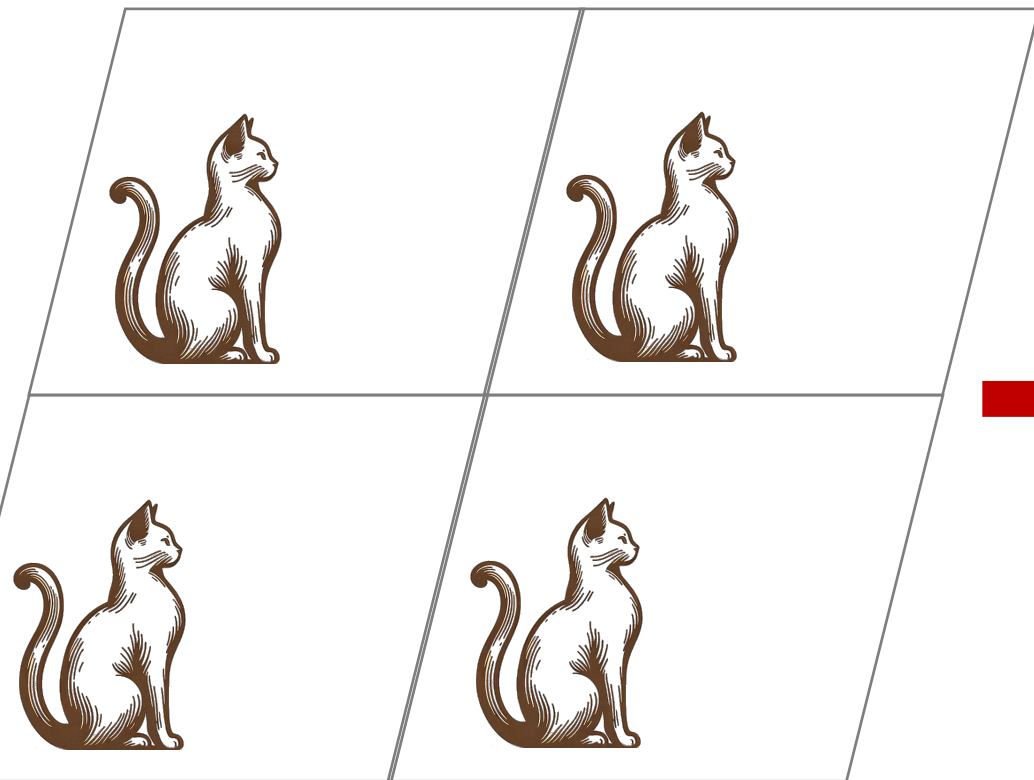
Crystal of unknown structure



Known model provides initial estimates of the phases of the unknown structure.

# Molecular Replacement (MR)

Crystal of unknown structure

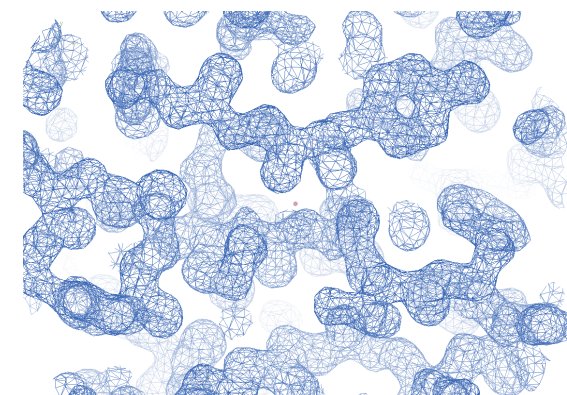


Intensities (hkl)



$$|F| e^{i\phi}$$

Known model

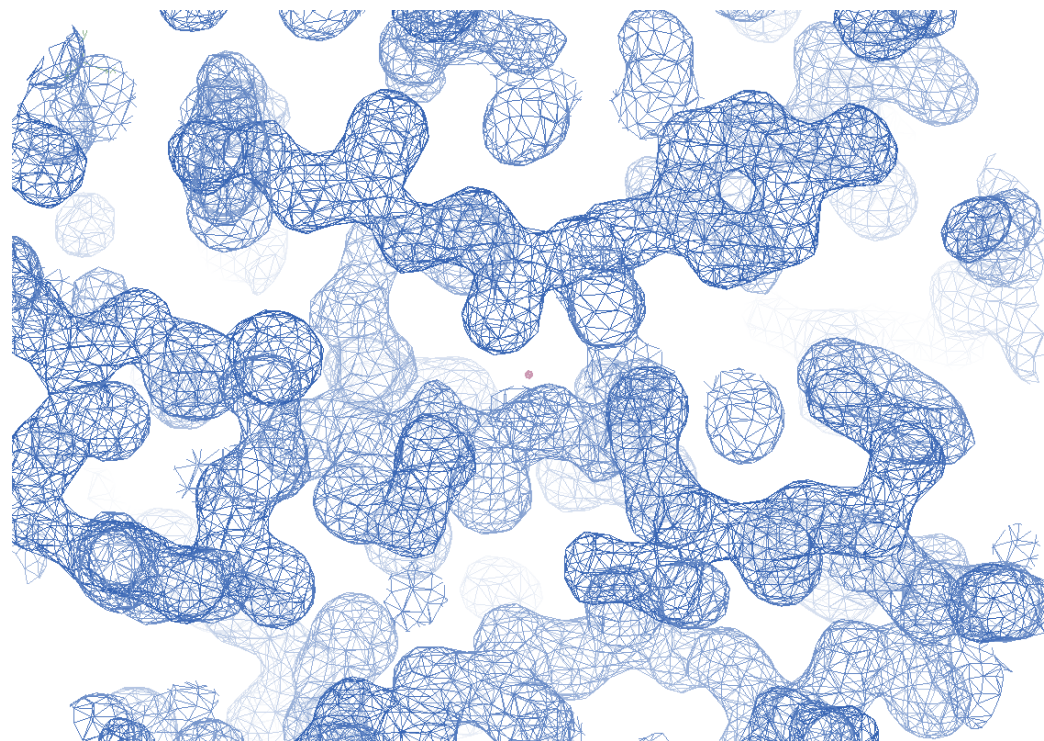


Density map



# Molecular Replacement (MR)

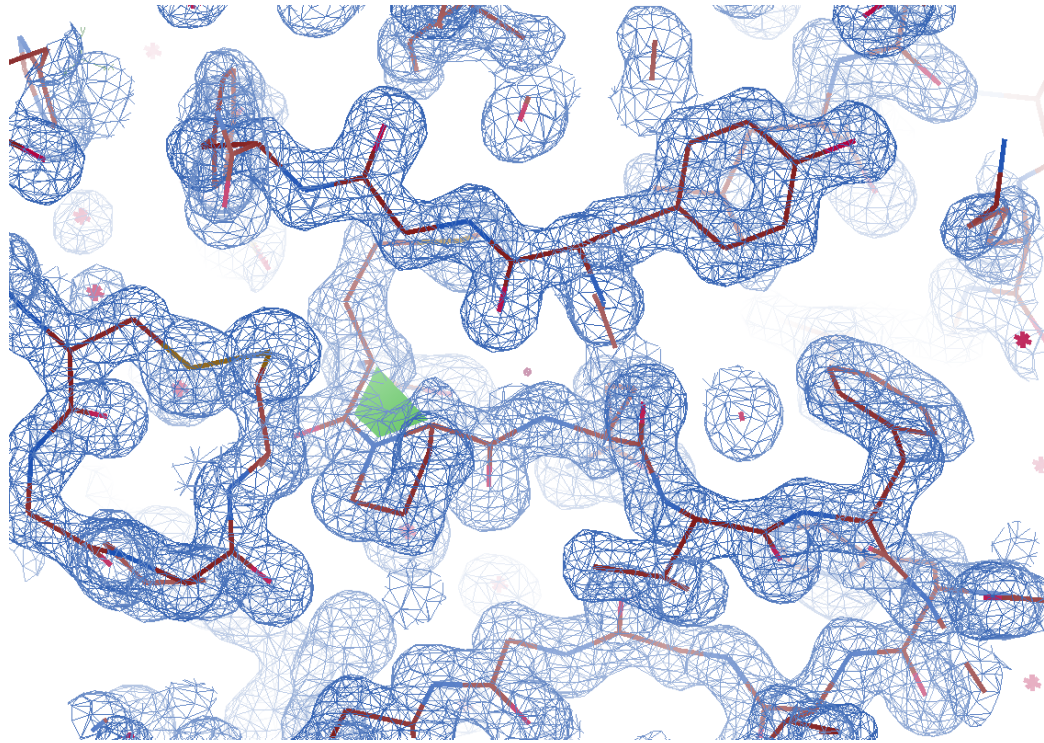
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If we know the density...

# Molecular Replacement (MR)

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If we know the density...

... then we can  
determine the structure

# MR will solve most structures

Try to solve recent SAD structures with MR and AF model.



## Accelerating crystal structure determination with iterative *AlphaFold* prediction

Thomas C. Terwilliger,<sup>a,b\*</sup> Pavel V. Afonine,<sup>c</sup> Dorothee Liebschner,<sup>c</sup> Tristan I. Croll,<sup>d</sup> Airlie J. McCoy,<sup>d</sup> Robert D. Oeffner,<sup>d</sup> Christopher J. Williams,<sup>e</sup> Billy K. Poon,<sup>c</sup> Jane S. Richardson,<sup>e</sup> Randy J. Read<sup>d</sup> and Paul D. Adams<sup>c,f</sup>

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OPEN ACCESS  
Cited by 2  
Part of a special issue

90% of 215 data sets solved with MR

97% of 406 data sets solved with MR  
(6% are “hard” cases)

## The success rate of processed predicted models in molecular replacement: implications for experimental phasing in the *AlphaFold* era

Ronan M. Keegan,<sup>a,b</sup> Adam J. Simpkin<sup>a</sup> and Daniel J. Rigden<sup>a\*</sup>

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Terwilliger, T. C. *et al.* *Acta Crystallogr. D Struct. Biol.* **79**, 234–244 (2023).

<https://doi.org/10.1107/S205979832300102X>

Keegan, R. M., Simpkin, A. J. & Rigden, D. J. *Acta Crystallogr. D Struct. Biol.* **80**, 766–779 (2024).

<https://doi.org/10.1107/S2059798324009380>

# Molecular replacement: Approach

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Try to match the known model with the unknown structure.



Search model

Crystal of unknown structure



Find the **rotation** and **translation** of the search model so that it matches the unknown structure.



# The search model

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- Finding a suitable search model is critical step in MR.
- Should provide a high proportion of the scattering from the target structure with high accuracy (low r.m.s.d.).

Crystal of unknown structure



# The search model

---

- Finding a suitable search model is critical step in MR.
- Should provide a **high proportion of the scattering** from the target structure with high accuracy (low r.m.s.d.).

Crystal of unknown structure



May not work  
Search model

Only small part of actual  
model

# The search model

---

- Finding a suitable search model is critical step in MR.
- Should provide a high proportion of the scattering from the target structure with **high accuracy (low r.m.s.d.)**.



Not similar to the target

Crystal of unknown structure



# What can be used as search model?

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Search model should be similar to the target structure.

## 1) **Homologue structure**

If the sequence is similar → structures may be similar

- Sequence comparison search
- Prune regions of large sequence diversity
- Truncate side-chains



Search model



Unknown structure



# What can be used as search model?

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## 1) **Homologue structure**

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Search model



Unknown structure

# What can be used as search model?

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Search model should be similar to the target structure.

## 2) Predicted structure (AlphaFold, RosettaFold)

Process the predicted model before MR:

- Remove low pLDDT regions
- Split into domains if necessary
- Convert pLDDT to B-factors

Unknown structure



Predicted model

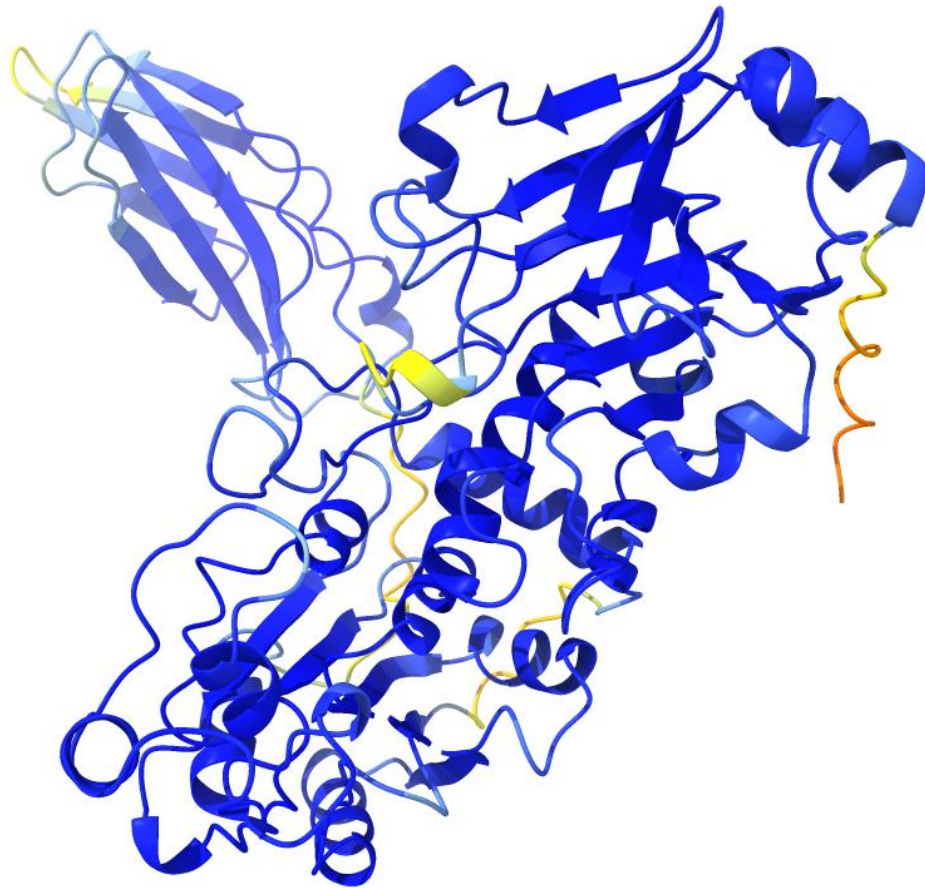


May have  
- Distortions  
- Incorrect domain  
relationships

# Using predicted models: B-factors

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Color by pLDDT



Color by B-factor



high pLDDT (high confidence)

low pLDDT (low confidence, uncertain)



high B-factor (disordered, uncertain)

low B-factor (ordered)

# Using predicted models: B-factors

---

high pLDDT (high confidence)

low pLDDT (low confidence, uncertain)



high B-factor (disordered, uncertain)

low B-factor (ordered)

B-factor may be used in downstream calculations, e.g. to calculate weights for docking. Residues with high B-factors are downweighed.

→ Convert pLDDT to pseudo B-factors.

$$\Delta = 1.5 \exp[4(0.7 - \text{pLDDT})]$$

$$B = \frac{8\pi^2 \Delta^2}{3}$$



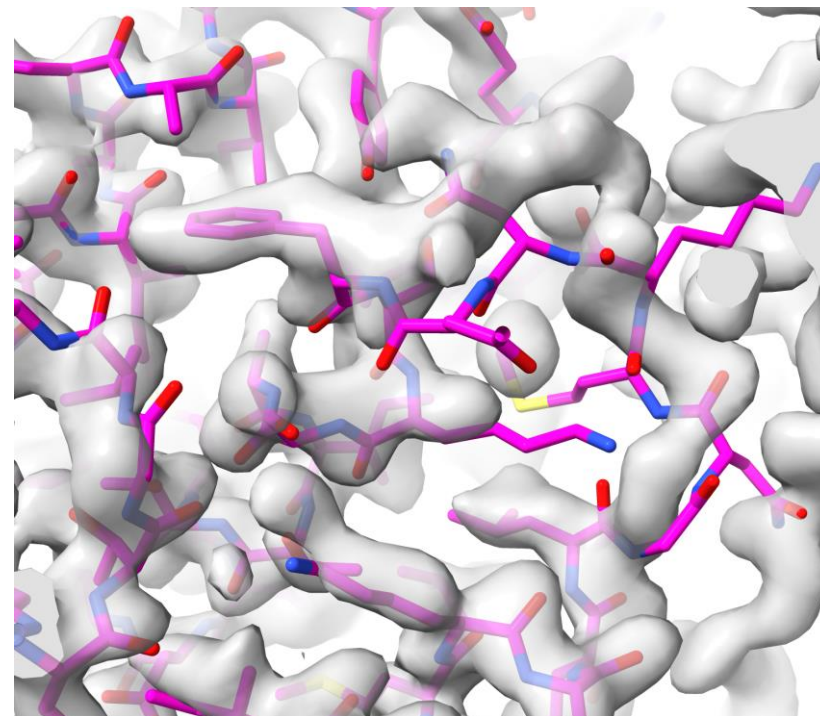
# Limitations of predicted models

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## AI/ML model predictions

- RNA/DNA not as accurate yet.
- High pLDDT regions are not necessarily correct.
- Know almost nothing about physics and chemistry.
- Generate a single structure, but no conformational changes (influenced by pH, temperature, ions, ligands, other proteins).

**Wrong  
prediction**



# Molecular replacement: Scoring

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Compare observed and calculated diffraction.



Poor score



Good score

Different approaches:

- Patterson function
- Maximum-likelihood Methods (Phaser)

# MR Scoring: Maximum Likelihood Method

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“For any postulated orientation and position of the model, what is the probability of obtaining the structure amplitudes that we observe?”



Explicitly models errors

- Experimental uncertainties
- r.m.s. coordinate error of the search model

→ Likelihood methods are more robust and generally give clearer solutions in difficult cases

# Maximum Likelihood Scoring in Phaser

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**LLG = Log Likelihood gain**

→ It measures how much better the data can be predicted with the search model than with a random distribution of the same atoms.

**TF-Z** = how many standard deviations your solution is above the mean (the higher the better).

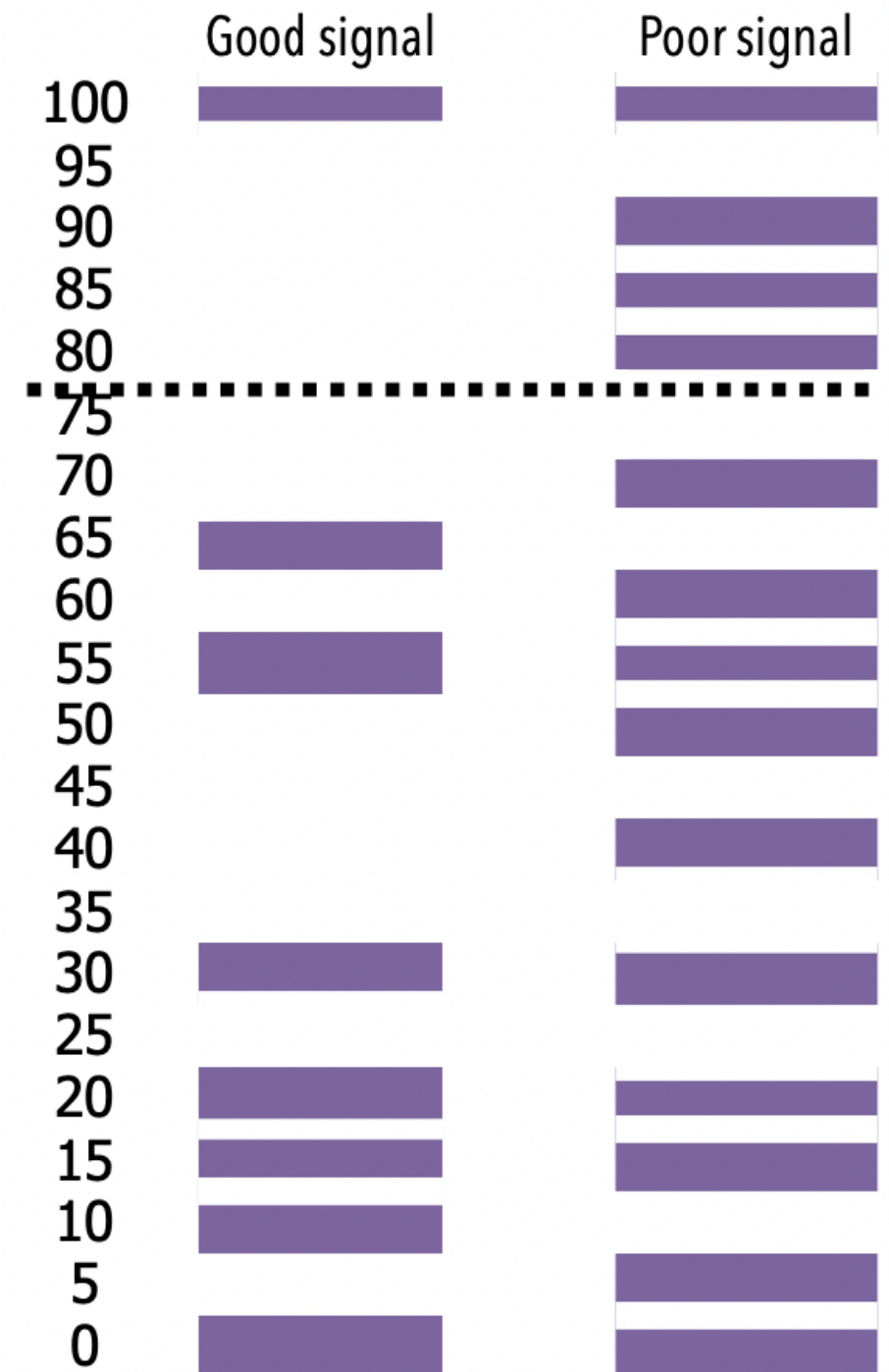


# Maximum Likelihood Scoring in Phaser

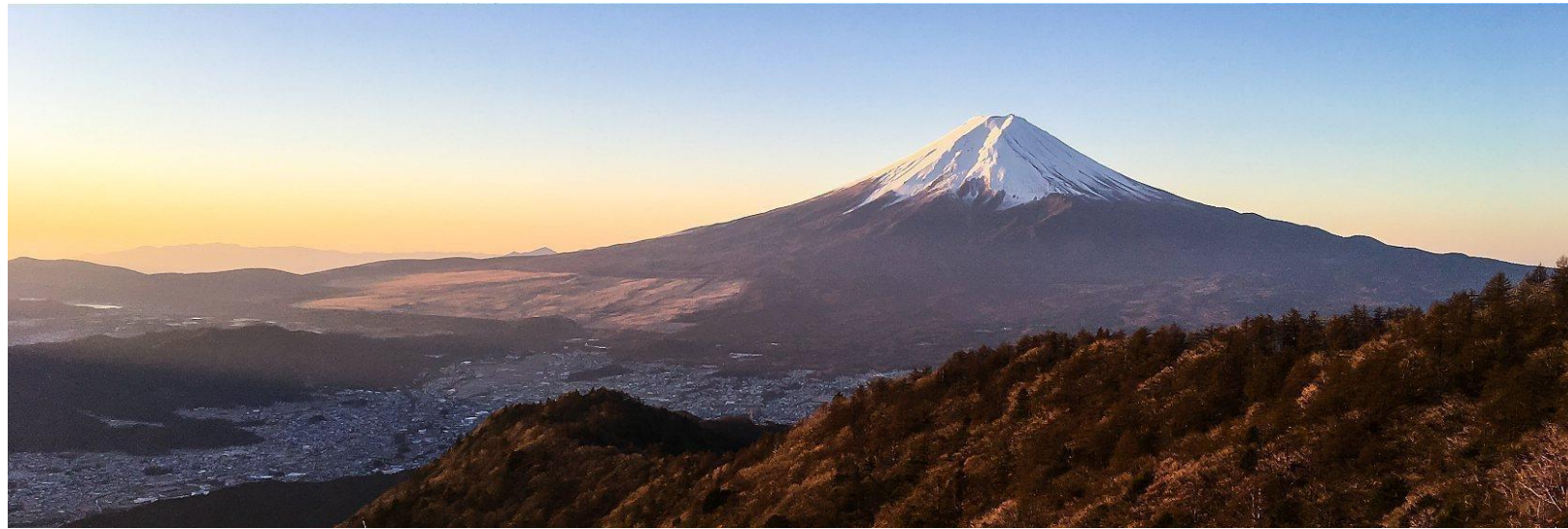
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Select solutions that are over 75% of the difference between the top peak and the mean.

- Good signal, few potential solutions
- Poor signal, many potential solutions



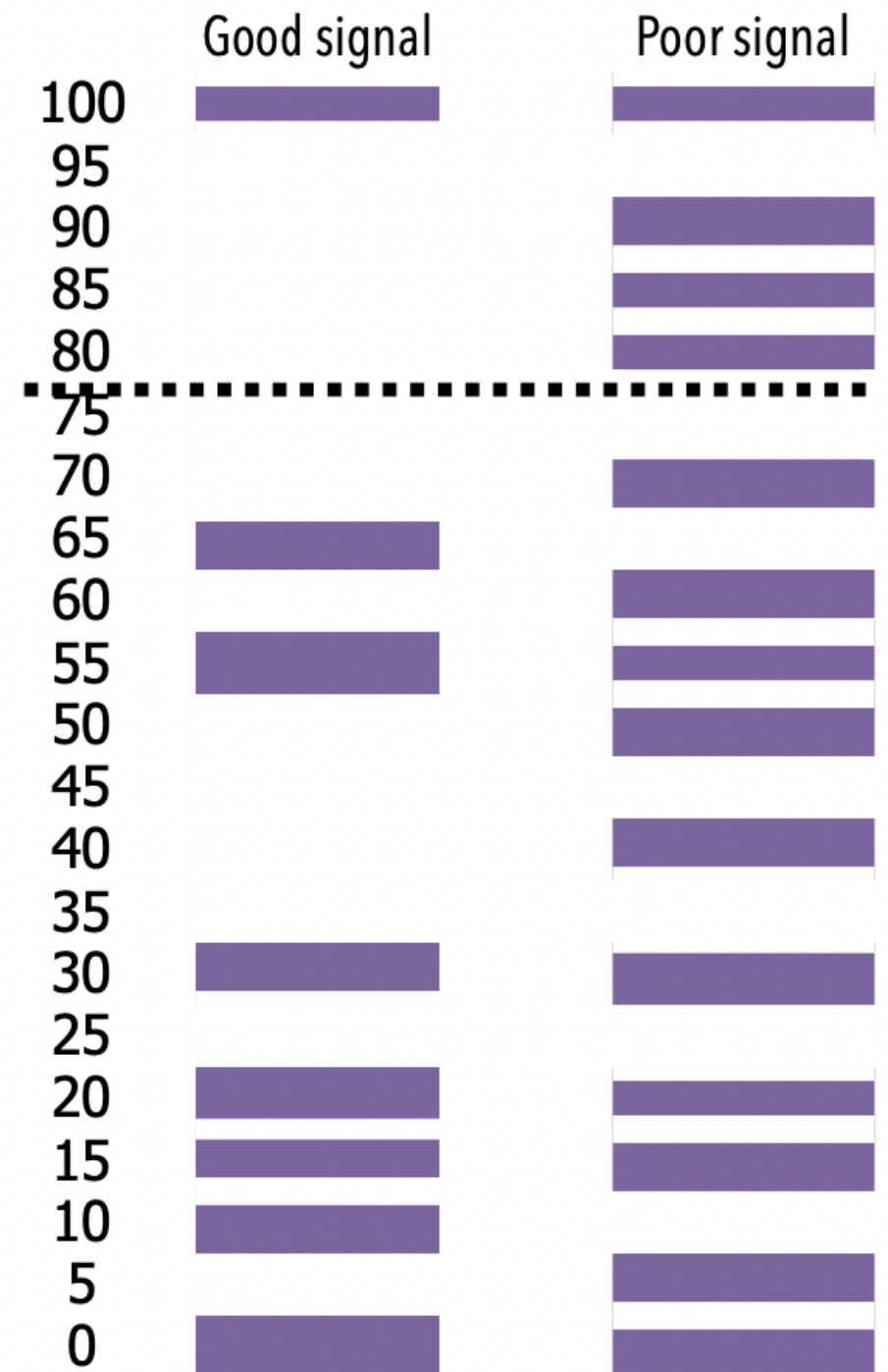
# Maximum Likelihood Scoring in Phaser



Good signal



Poor signal



# Maximum Likelihood Scoring in Phaser

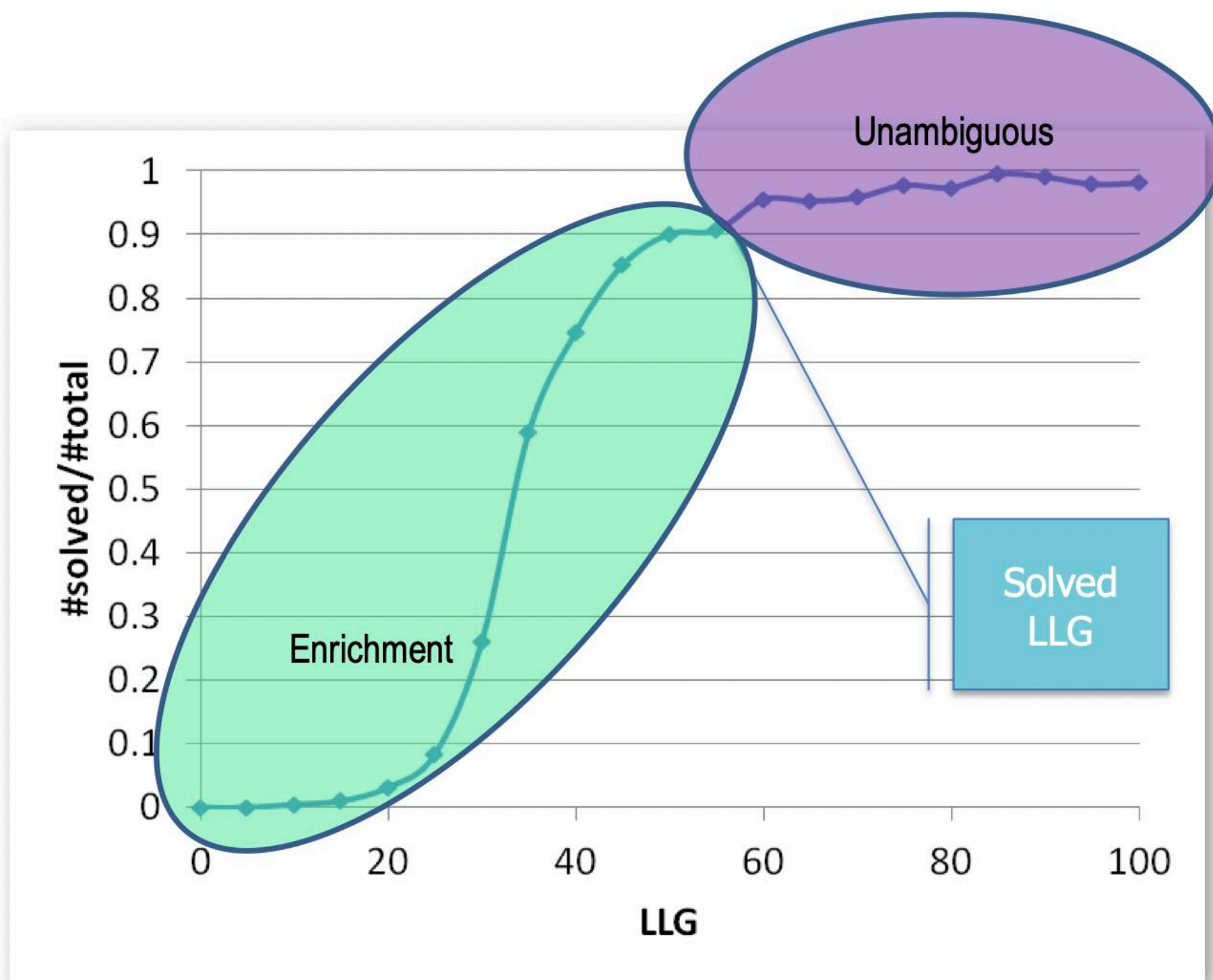
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TF Z-score	LLG score	Solved?
< 5	< 25	no
5 - 6	25 - 36	unlikely

6 - 7	<div>Summary</div> <div><b>Phaser has found 1 MR solution(s).</b></div> <div><b>Top LLG:</b> 11480.402</div> <div><b>Top TFZ:</b> 68.1</div> <div><b>Spacegroup:</b> C 1 2 1</div>	
7 - 8		
> 8		



# Maximum Likelihood Scoring in Phaser



Database of  
over 23000  
MR problems

Plot of LLG versus success in structure solution

*R.D. Oeffner*

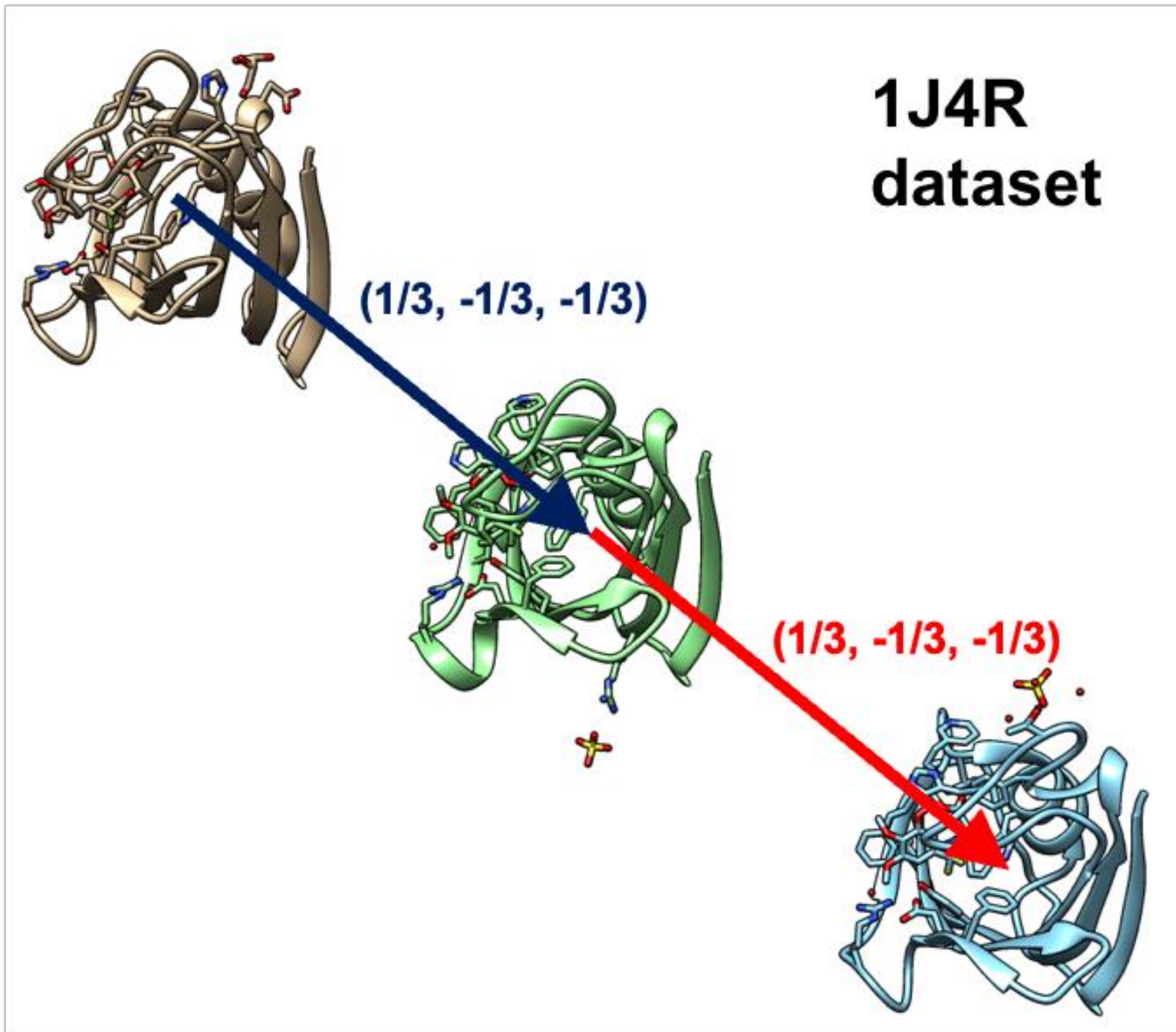
# Likelihood is sensitive...

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- ...to correct orientation and position of molecular replacement model
  - successful in solving structures with distant relatives, small fragments, or many copies in asymmetric unit
- ...to violations of assumptions
  - data implicitly assumed to be isotropic  
→ important to account for anisotropy
  - tNCS: intensity distribution is modulated
  - components may not be equally well-ordered  
→ important to correct for differences in overall B-factors

# Translational NCS

Two or more copies of the molecule are related by pure translation.



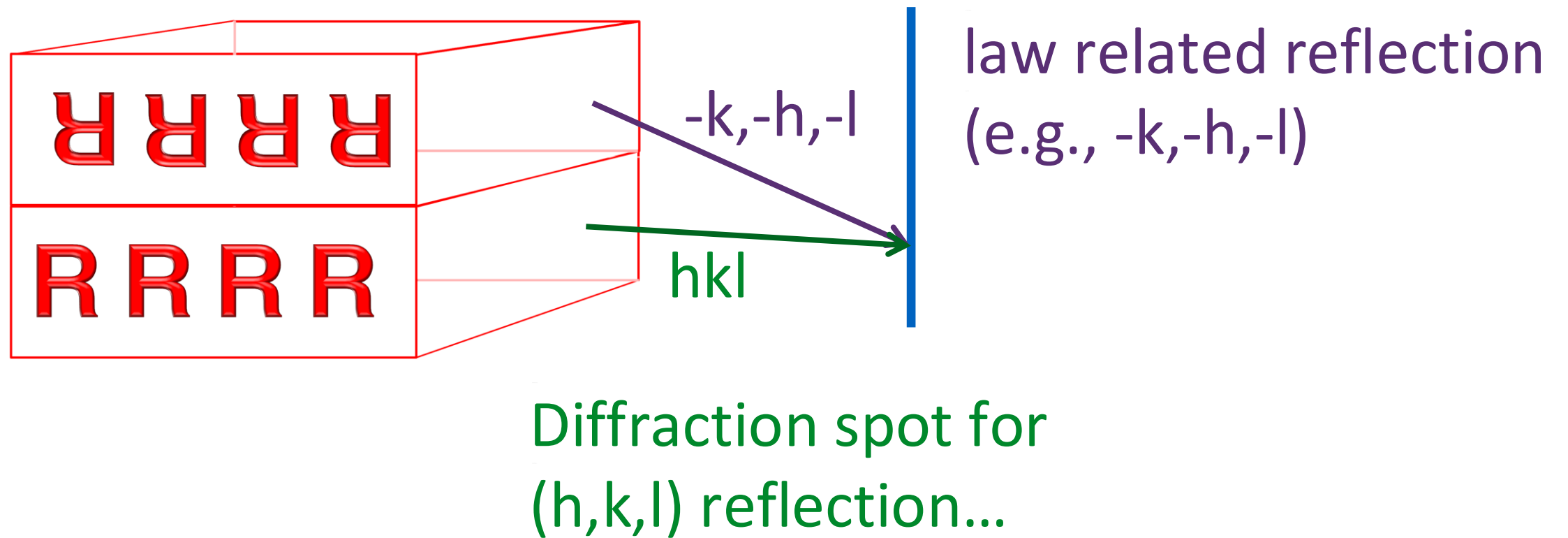
Strong peak in  
Patterson function

In this case at  
 $(1/3, -1/3, -1/3)$

# Twinning

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Identical but rotated crystals sandwiched together

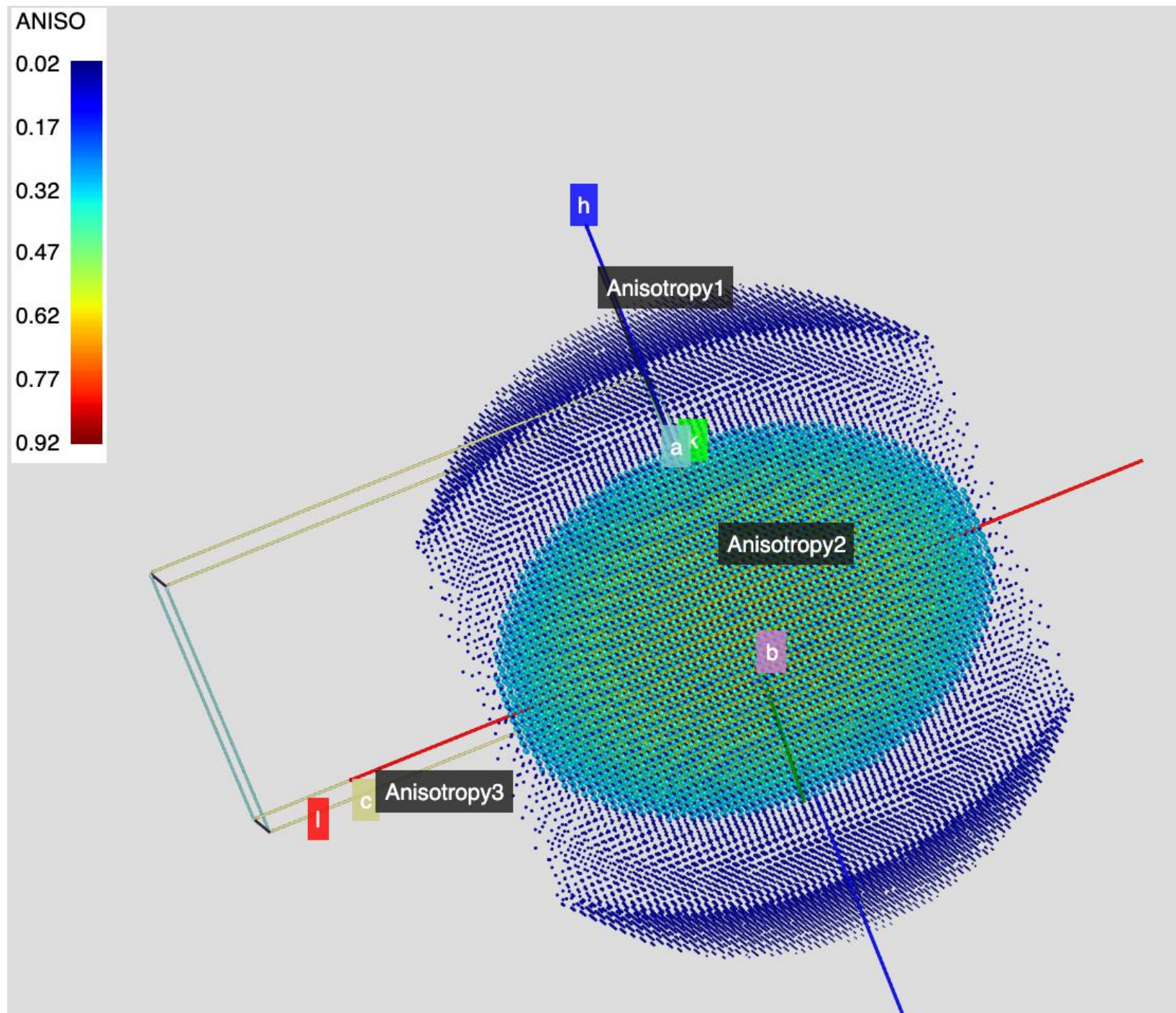


Possible twin laws depend on your crystal symmetry and cell dimensions



# Anisotropic data

Crystal does not diffract equally well in all directions.



Phaser takes care of anisotropy corrections  
→ No need to truncate  
(Truncating may confuse Phaser's intensity analyses)



# What is needed to run Phaser MR

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- Reflection data
- Search model
- Error estimation of the search model
  - Homologue: sequence identity
  - Predicted model: r.m.s.d. (1.0 Å)
- ASU content:
  - Sequence of the construct
  - How many copies of the molecule(s)
- Awareness of data pathologies:
  - Twinning
  - tNCS
  - anisotropy

# If MR does not work

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- Double check space group (twinning).
- Does your data set have uncurable pathologies?  
(low resolution, high mosaicity)
- Is the content correct (e.g., impurities)?  
Is it the correct sequence file?
- Can the search model be improved?
  - is the search model complete enough (AF multimer)?
  - use other prediction software.
  - use a different splitting method.
- Use secondary structure based software
  - ARCIMBOLDO, AMPLE
- Discuss with your colleagues; ask at bulletin boards (ccp4bb); ask software developers

# The Project



## Lawrence Berkeley Laboratory

Paul Adams, Pavel Afonine,  
Dorothee Liebschner, Nigel  
Moriarty, Billy Poon,  
Christopher Schlicksup,  
Oleg Sobolev



## University of Cambridge

Randy Read, Airlie McCoy,  
Alisia Fadini



## Los Alamos National Laboratory New Mexico Consortium

Tom Terwilliger, Li-Wei Hung



## UTHealth

Matt Baker



## Duke University

Jane & David Richardson,  
Christopher Williams,  
Vincent Chen



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